



Variable density low-Mach number solver (VDS)

V. Moureau, G. Lartigue, P. Bénard
CNRS-CORIA, UMR 6614, Rouen
<http://www.coria-cfd.fr>

Projection method

Projection method

- The variable density projection method is an extension of the Chorin method (Pierce and Moin 2004)

- Prediction

$$\frac{\rho \mathbf{u}^* - \rho \mathbf{u}^n}{\Delta t} + \nabla \cdot (\rho \mathbf{u}^{n+1/2} \mathbf{u}^{n+1/2}) = 0$$

- Correction

$$\frac{\rho \mathbf{u}^{n+1} - \rho \mathbf{u}^*}{\Delta t} = -\nabla P^{n+1/2}$$

Poisson equation

$$\nabla \cdot \nabla P^{n+1/2} = \frac{\rho^{n+3/2} - \rho^{n+1/2}}{\Delta t^2} + \frac{1}{\Delta t} \nabla \cdot (\rho \mathbf{u}^*)$$

- And the density has to be prescribed from

Equation of state

- The big difference between constant density and variable density methods is the equation of state, which gives the density

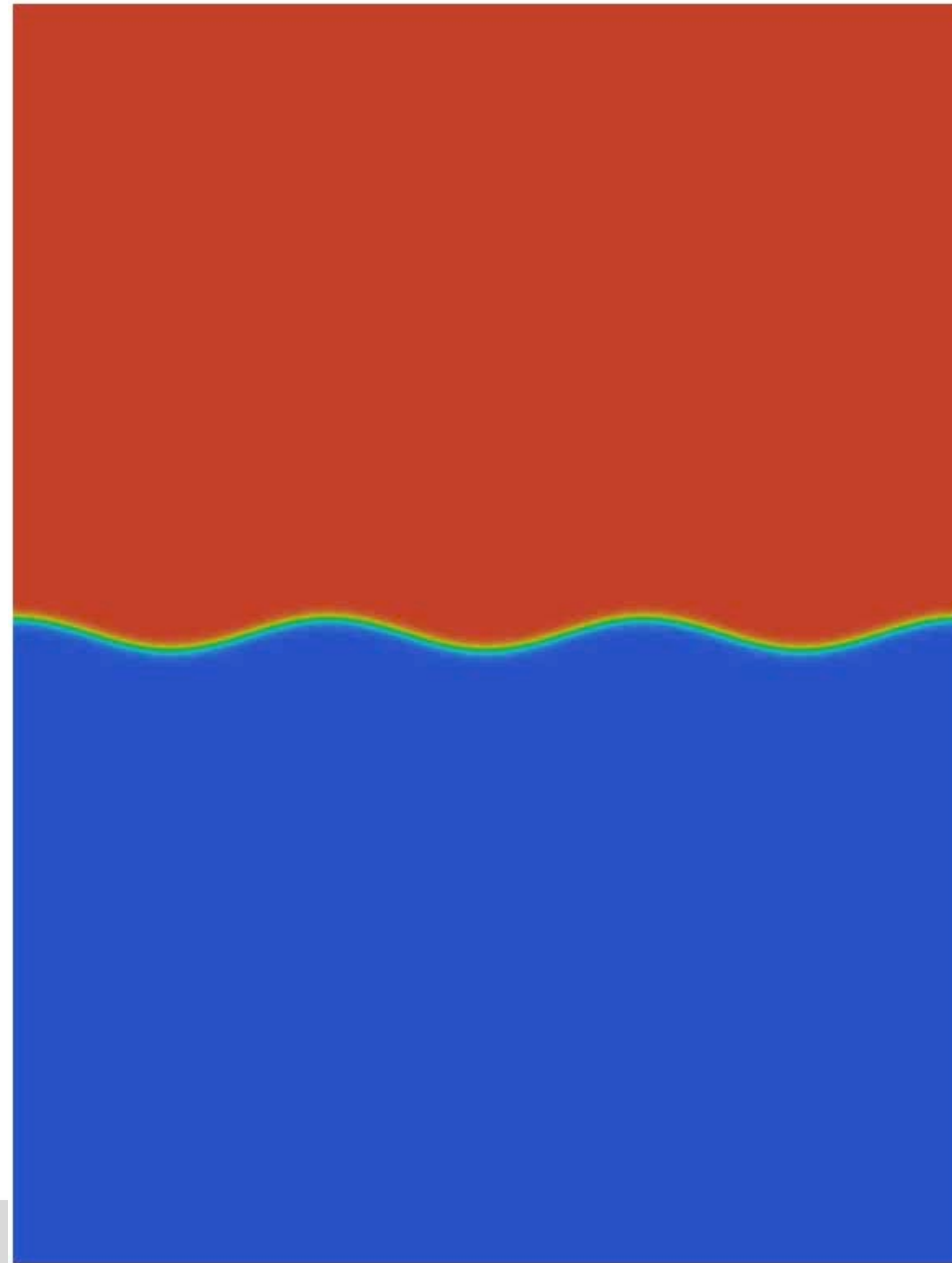
$$\rho^{n+3/2} = f(P_0, c^{n+3/2}, z^{n+3/2}, \dots)$$

- In **YALES2**, several EOS are available
 - EOS_TYPE_CONSTANT_DENSITY
 - EOS_TYPE_PURE_MIXING
 - EOS_TYPE_MULTI_SPECIES_MIXING
 - EOS_TYPE_MIXED_IS_BURNED
 - EOS_TYPE_ONE_STEP
 - EOS_TYPE_RHO_AND_T_FROM_1D_TABLE
 - EOS_TYPE_CHEMTABLE
 - EOS_TYPE_IDEAL_GAS
 - EOS_TYPE_MULTISPECIES_GAS
 - EOS_TYPE_FTACLES

Mixing test case

avvt/vds_Rayleigh_Taylor

- Mixing of two fluids with different densities



avvt/vds_Rayleigh_Taylor

- Temporal loop

```
SOLVER_NAME = 'Rayleigh_Taylor'  
SOLVER_TYPE = VARIABLEDENSITY  
NDIM = 2  
NITER_MAX = 500  
DUMP_NITER_PERIOD = 5  
CFL = 0.9  
FOURIER = 0.2  
GRAVITY_NUMBER = 0.1  
ITER_INFO_PERIOD = 5
```

- Physical properties

```
DYNAMIC_VISCOSITY = 3.13E-4  
GRAVITY = 0.0 -9.81 0.0
```

- Mixture fraction

```
SCALAR Z TYPE = PASSIVE
```

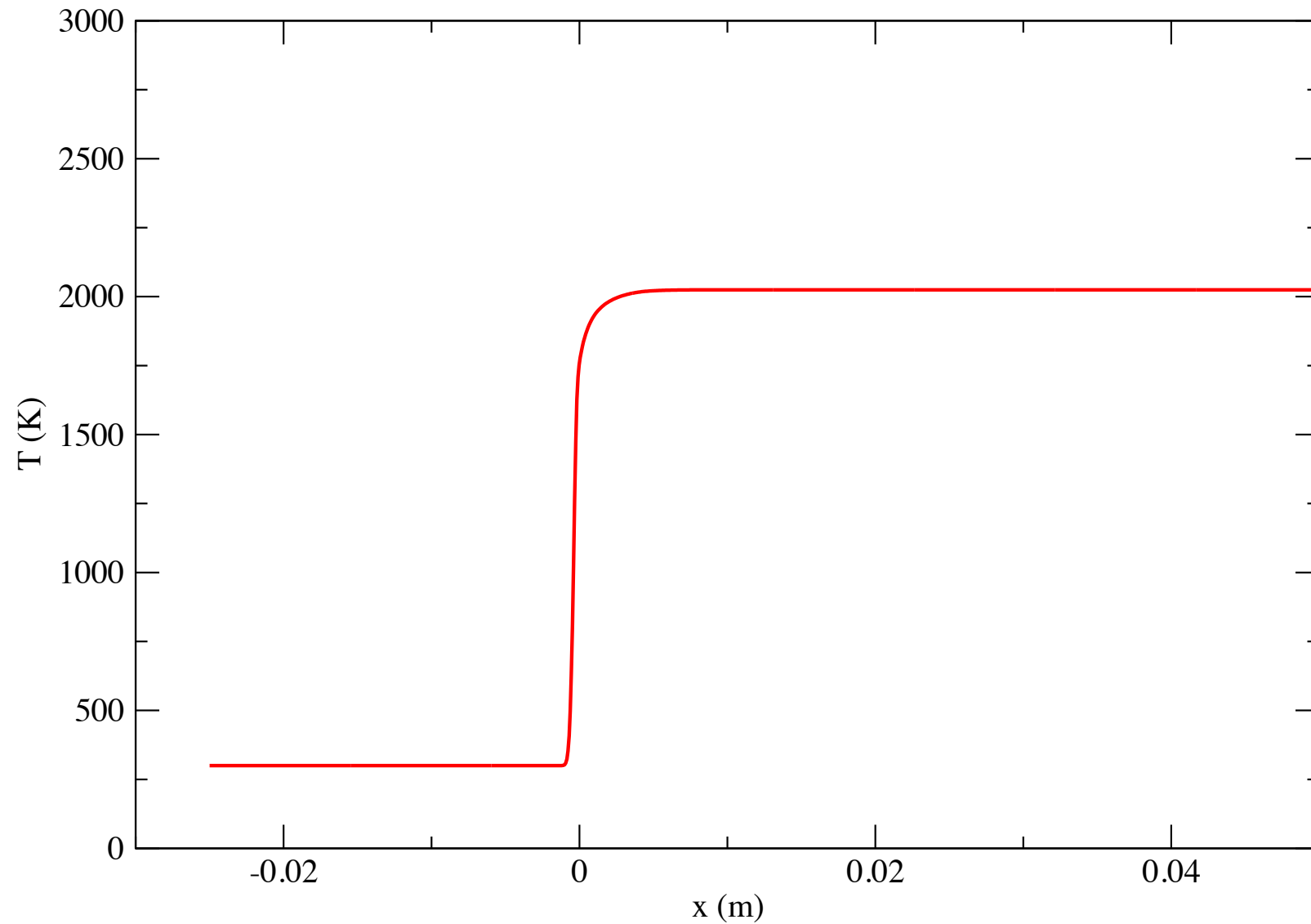
- Equation of state

```
EOS_TYPE = PURE_MIXING  
EOS_RHO0 = 0.1694  
EOS_RHO1 = 1.225  
EOS_T0 = 2169.4  
EOS_T1 = 300.0
```

1D flame

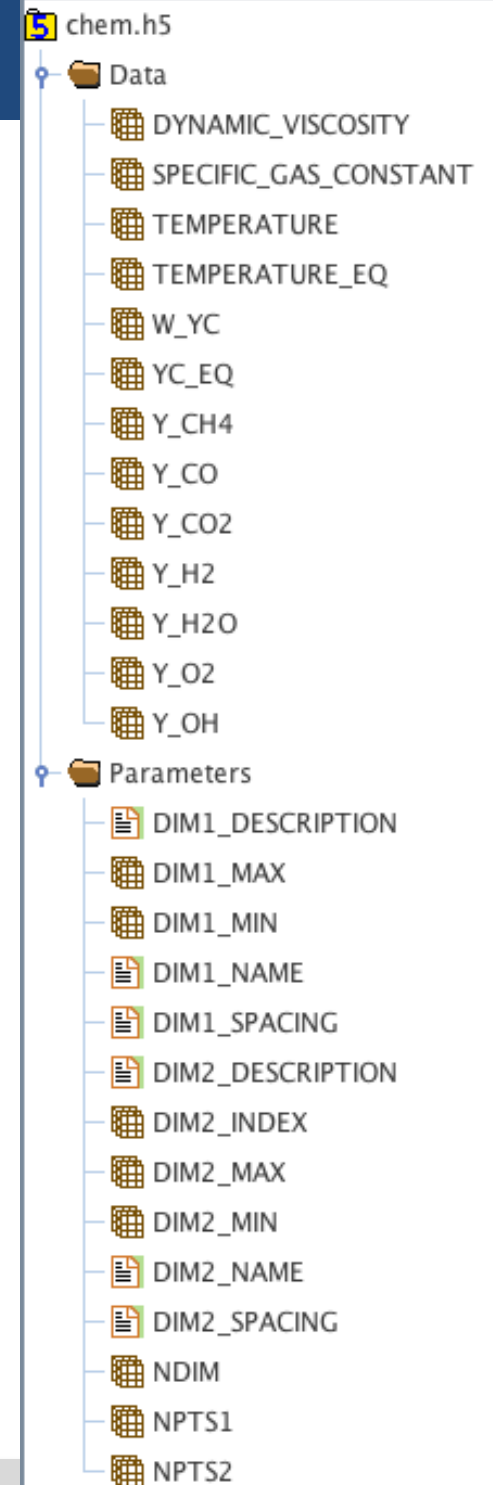
avvt/vds_1D_flame_FPI_methane

- Tabulated chemistry 1D flame (FPI)



avvt/vds_1D_flame_FPI_methane

- Laminar look-up table
 - example in aqat/chemtable/table/chem.h5
- Turbulent look-up table
 - Can be convoluted by PDFs in aqat/chemtable
- Important parameters
 - $NDIM = 2$
 - $DIM1_NAME = C$
 - $NPTS1 = 300$
 - $DIM2_NAME = Z$
 - $NPTS2 = 51$
- YALES2 will try to find C and Z in the data list
- Number of dimensions from 1 to 6.



avvt/vds_1D_flame_FPI_methane

- Temporal loop

```
SOLVER_NAME = '1D air/methane flame at phi=0.83'  
SOLVER_TYPE = VARIABLEDENSITY  
NDIM = 1  
CFL = 1.5  
FOURIER = 0.3  
NITER_MAX = 10000  
DUMP_NITER_PERIOD = 100  
ITER_INFO_PERIOD = 5  
IMPLICIT_DIFFUSION = TRUE
```

- Physical properties

```
TURBULENCE_MODEL = NONE  
MOLECULAR_VISCOSITY_TYPE = SUTHERLAND
```

- Scalars

```
SCALAR Z TYPE = CONSTANT  
SCALAR Z VALUE = 0.04565  
SCALAR YC TYPE = PROGRESS_VARIABLE  
SCALAR YC ST_TYPE = CHEMTABLE  
SCALAR YC SC = 0.72  
SCALAR Y_OH TYPE = POSTPROC  
SCALAR Y_OH POSTPROC_TYPE = CHEMTABLE  
SCALAR Y_CO TYPE = POSTPROC  
SCALAR Y_CO POSTPROC_TYPE = CHEMTABLE  
SCALAR Y_CO2 TYPE = POSTPROC  
SCALAR Y_CO2 POSTPROC_TYPE = CHEMTABLE
```

avvt/vds_1D_flame_FPI_methane

- EOS

```
EOS_TYPE = CHEMTABLE
CHEMTABLE_FORMAT = HDF
CHEMTABLE_FILE = '../..//aqat/chemtable/table/filtered_chemtable.h5'
CHEMTABLE_DIM1_TRANSPORTED_NAME = "YC"
CHEMTABLE_DIM1_NEEDS_RESCALING = "TRUE"
```

- “rescaling” consists in dividing YC by YC_EQ, which is also in the table

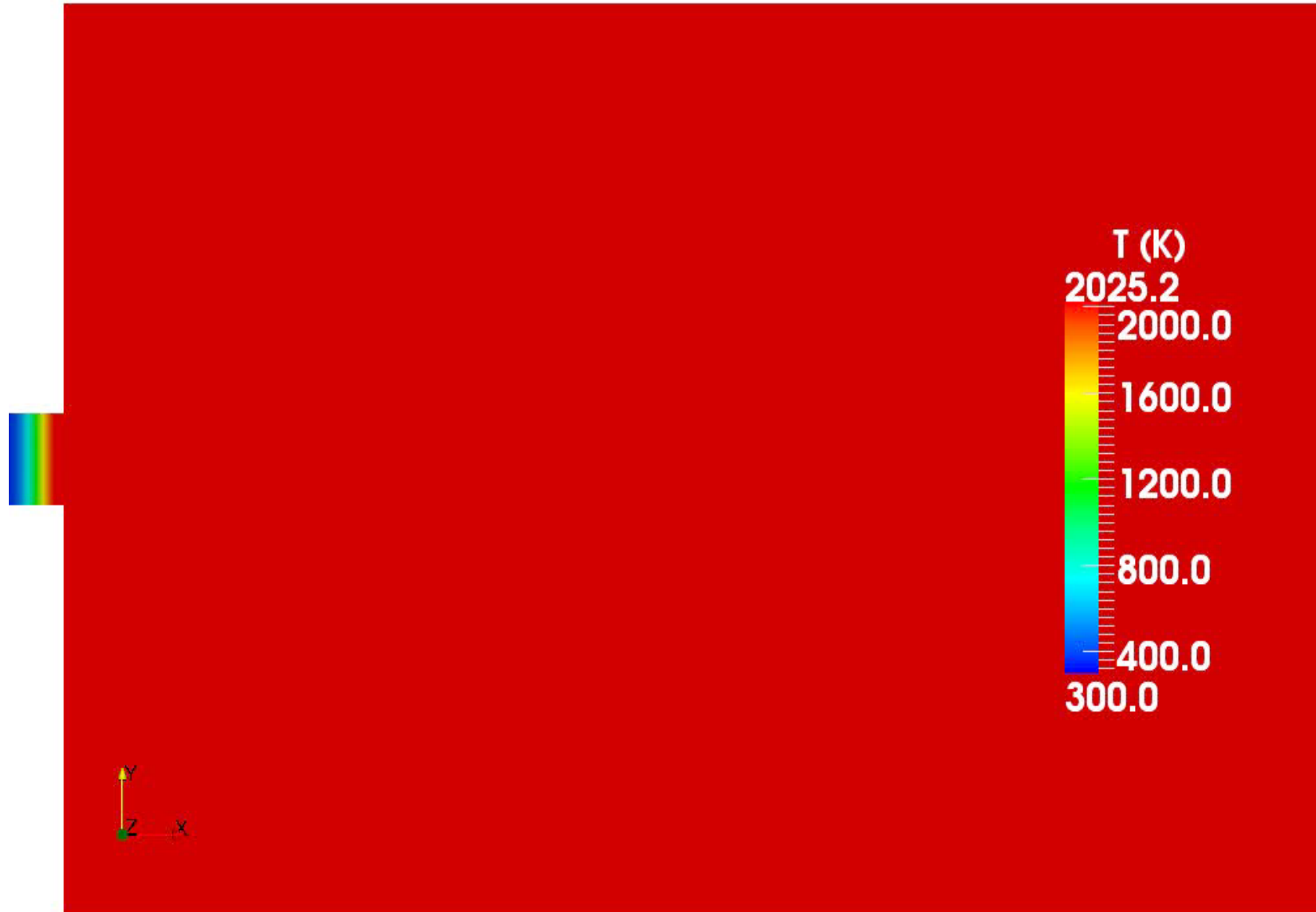
- Additional parameters

```
#CHEMTABLE_INTERPOLATION_TYPE = LINEAR
CHEMTABLE_INTERPOLATION_TYPE = CUBIC # default
#CHEMTABLE_INTERPOLATION_TYPE = MONOTONIC_CUBIC
```

Turbulent flame with tabulated chemistry (PCM-FPI)

avvt/vds_2D_bunsen_flame

- 2D turbulent flame with PCM-FPI (Domingo et al. 2008)



avvt/vds_2D_bunsen_flame

- Temporal loop

```
SOLVER_NAME = '1D air/methane flame at phi=0.83'  
SOLVER_TYPE = VARIABLEDENSITY  
NDIM = 2  
CFL = 1.0  
FOURIER = 0.2  
NITER_MAX = 10000  
DUMP_NITER_PERIOD = 100  
ITER_INFO_PERIOD = 5  
IMPLICIT_DIFFUSION = TRUE
```

- Physical properties

```
TURBULENCE_MODEL = NONE  
MOLECULAR_VISCOSITY_TYPE = SUTHERLAND
```

- EOS

```
EOS_TYPE = CHEMTABLE  
CHEMTABLE_FORMAT = HDF  
CHEMTABLE_FILE = '../..//aqat/chemtable/table/filtered_chemtable.h5'  
CHEMTABLE_DIM1_TRANSPORTED_NAME = "YC"  
CHEMTABLE_DIM1_NEEDS_RESCALING = "TRUE"
```

avvt/vds_2D_bunsen_flame

- Scalars

```
SCALAR Z TYPE = CONSTANT  
SCALAR Z VALUE = 0.04565
```

```
SCALAR YC TYPE = PROGRESS_VARIABLE  
SCALAR YC ST_TYPE = CHEMTABLE  
SCALAR YC SC = 0.72
```

```
SCALAR YC_EQ TYPE = POSTPROC  
SCALAR YC_EQ POSTPROC_TYPE = CHEMTABLE
```

```
SCALAR S_C TYPE = POSTPROC  
SCALAR S_C POSTPROC_TYPE = UNMIXEDNESS  
SCALAR S_C MODEL = MIXING  
#SCALAR S_C MODEL = GRADIENT  
SCALAR S_C SOURCE = YC  
SCALAR S_C RESCALING_VARIABLE = YC_EQ
```

```
# algebraic model  
# other algebraic model
```

```
SCALAR Y_OH TYPE = POSTPROC  
SCALAR Y_OH POSTPROC_TYPE = CHEMTABLE  
SCALAR Y_CO TYPE = POSTPROC  
SCALAR Y_CO POSTPROC_TYPE = CHEMTABLE  
SCALAR Y_CO2 TYPE = POSTPROC  
SCALAR Y_CO2 POSTPROC_TYPE = CHEMTABLE
```


NOx model

- For the NOx model of Pecquery et al. (2014), an additional look-up table is required, which contains the source terms for NO transport equation

```
NOMANI_MODEL = TRUE  
NOMANI_NO_TABLE = 'table/sandia_D_400z_300c.h5'
```

- The model creates automatically the Y_NO scalar of type PROGRESS_VARIABLE with source term of type NOMANI
- The user only needs to specify
 - Y_NO on the inlets
 - W_NO has to be in the FPI look-up table (CHEMTABLE)